

II INTERNATIONAL CONFERENCE  
KRASNOYARSK, RUSSIA  
16-18 April 2020



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Modernization, Innovations, Progress:  
Advanced Technologies in Material Science,  
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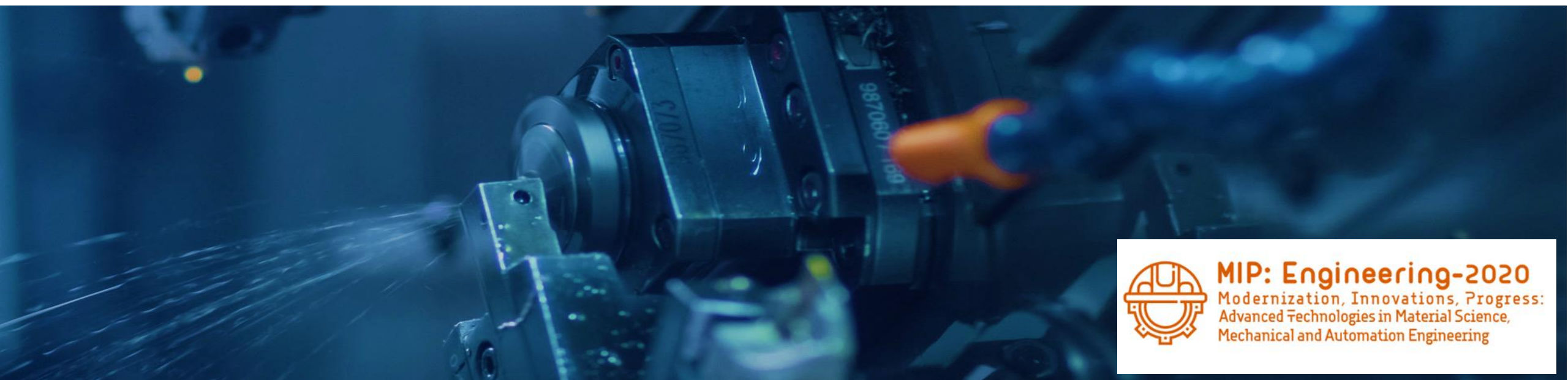
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**«Numerical modeling of viscous currents near axial symmetric surfaces»**

M.M. Gorokhov, A.V. Korepanov, V.A. Tenenev, S.V. Vologdin

# Problem statement

- Flow study near axial symmetric surfaces divides to subcritical and supercritical Reynolds numbers
- In the range of supercritical Reynolds numbers flow changes from laminar to turbulent
- Task: describe mathematical model for Reynolds number more than  $2 \cdot 10^5$



# Solution methods

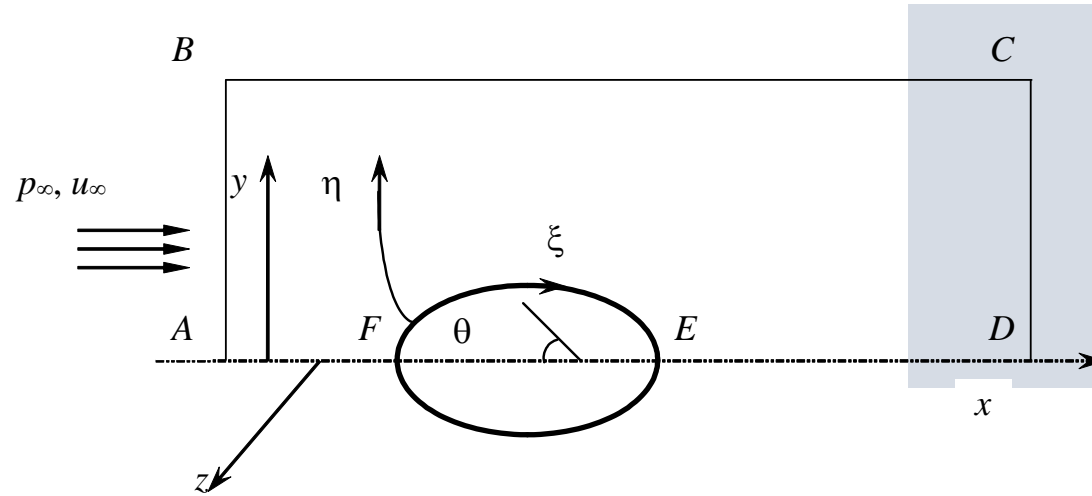


Figure 1. Range of integration



# Solution methods

$(\xi, \eta)$  - orthogonal curvilinear axial symmetric system of coordinates

$$\mathbf{F}_\xi + \mathbf{G}_\eta = \mathbf{P} + \mathbf{R}_\xi + \mathbf{H}_\eta + \mathbf{S},$$

$$\mathbf{F} = yDU \begin{bmatrix} \rho \\ \rho u \\ \rho v \end{bmatrix}, \quad \mathbf{G} = yDV \begin{bmatrix} \rho \\ \rho u \\ \rho v \end{bmatrix}, \quad \mathbf{P} = -y \begin{bmatrix} 0 \\ p_\xi x_\xi - p_\eta y_\xi \\ p_\xi y_\xi + p_\eta x_\xi \end{bmatrix}, \quad \mathbf{R} = y\mu \begin{bmatrix} 0 \\ u_\xi \\ v_\xi \end{bmatrix}, \quad \mathbf{H} = y\mu \begin{bmatrix} 0 \\ u_\eta \\ v_\eta \end{bmatrix},$$

$$\mathbf{S} = \begin{bmatrix} 0 \\ -\mu_\xi(vx_\xi + yv_\eta) + \mu_\eta(vy_\xi + yv_\xi) \\ \mu_\xi(-vy_\xi + yu_\eta) - \mu_\eta(vx_\xi + yu_\xi) \end{bmatrix}, \quad U = \frac{1}{D}(ux_\xi + vy_\xi), \quad V = \frac{1}{D}(-uy_\xi + vx_\xi), \quad D = x_\xi^2 + y_\eta^2.$$



# Solution methods

One-equation turbulence model don't give adequate results. Consider next two-equation turbulence model. Numerical algorithm based on *SIMPLE*.

$$\mathbf{F} = yDU \begin{bmatrix} \rho E \\ \rho \varepsilon \end{bmatrix}, \quad \mathbf{G} = yDV \begin{bmatrix} \rho E \\ \rho \varepsilon \end{bmatrix}, \quad \mathbf{R} = y\mu \begin{bmatrix} E_\xi \\ \varepsilon_\xi \end{bmatrix}, \quad \mathbf{H} = y\mu \begin{bmatrix} E_\eta \\ \varepsilon_\eta \end{bmatrix}, \quad \mathbf{S} = yD \begin{bmatrix} \mu_T Q - \rho \varepsilon \\ c_\mu c_1 Q E - c_2 \rho \frac{\varepsilon^2}{E} \end{bmatrix},$$

$$c_1 = 1,44, \quad c_2 = 1,92, \quad c_\mu = 0,09; \quad \mu_T = c_\mu E^2 / \varepsilon,$$



# Solution methods

Finite-difference grid was generate using method based on solving Laplace equation (conformal map)

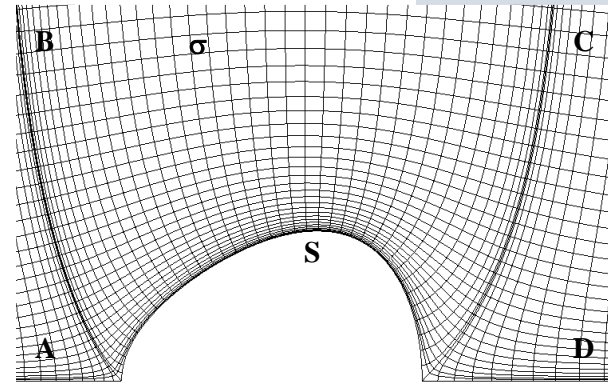


Figure 2. Curvilinear grid



# Solution methods

Simulated results are very closely to experimental

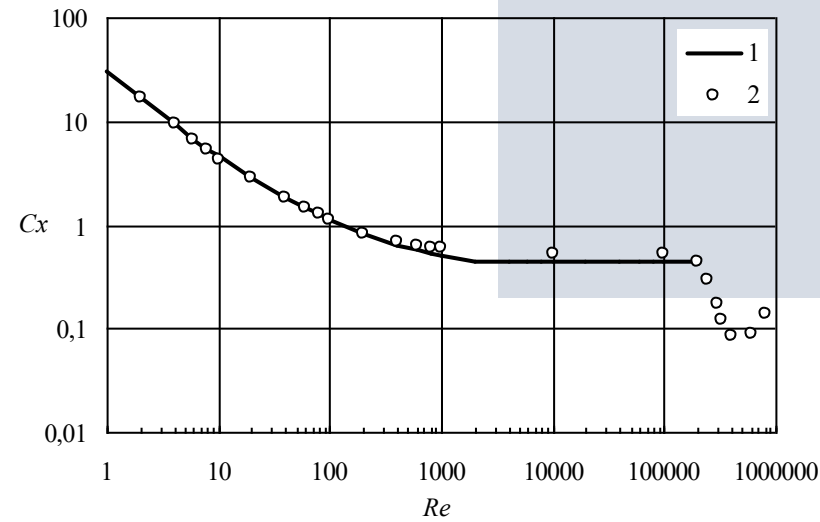


Figure 3. Drag coefficient as function of Reynolds number



# Solution methods

Visual results shown at fig.4 and fig.5

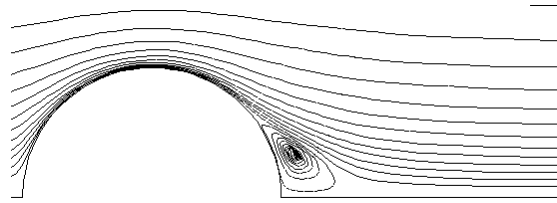


Figure 4. Sphere

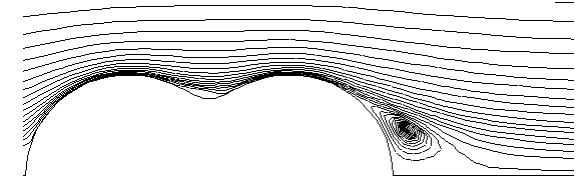


Figure 5. "dumbbell"







# Conclusions

Results, implementation

Shown mathematical model adequately describe boundary layer physical processes near axial symmetric surfaces.

Could be used to:

- solve turbulent erosive burning;
- calculate flow parameters;
- modelling turbulent flows.

# Contacts

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